

Differential Calculus

Function

Derivative

$$y = f(x)^n \quad \downarrow \text{power} \times \text{front} \quad \frac{dy}{dx} = n f'(x) [f(x)]^{n-1}$$

$$y = uv \quad \text{product rule} \quad \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$y = g(u) \quad \text{chain rule where } u = f(x) \quad \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

$$y = \frac{u}{v} \quad \text{quotient rule} \quad \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

$$y = \sin f(x) \quad \sin \rightarrow \cos \quad \frac{dy}{dx} = f'(x) \cos f(x)$$

$$y = \cos f(x) \quad \cos \rightarrow -\sin \quad \frac{dy}{dx} = -f'(x) \sin f(x)$$

$$y = \tan f(x) \quad \tan \rightarrow \sec^2 x \quad \frac{dy}{dx} = f'(x) \sec^2 f(x)$$

$$y = e^{f(x)} \quad \frac{dy}{dx} = f'(x) e^{f(x)}$$

$$y = \ln f(x) \quad \frac{dy}{dx} = \frac{f'(x)}{f(x)}$$

$$y = a^{f(x)} \quad \frac{dy}{dx} = (\ln a) f'(x) a^{f(x)}$$

$$y = \log_a f(x) \quad \frac{dy}{dx} = \frac{f'(x)}{(\ln a) f(x)}$$

$$y = \sin^{-1} f(x) \quad \frac{dy}{dx} = \frac{f'(x)}{\sqrt{1 - [f(x)]^2}}$$

$$y = \cos^{-1} f(x) \quad \frac{dy}{dx} = -\frac{f'(x)}{\sqrt{1 - [f(x)]^2}}$$

$$y = \tan^{-1} f(x) \quad \frac{dy}{dx} = \frac{f'(x)}{1 + [f(x)]^2}$$

Integral Calculus

$$\int f'(x) [f(x)]^n dx = \frac{1}{n+1} [f(x)]^{n+1} + c$$

$\uparrow$ power $\div$ new power where $n \neq -1$

$$\int f'(x) \sin f(x) dx = -\cos f(x) + c$$

$\sin \rightarrow -\cos$

$$\int f'(x) \cos f(x) dx = \sin f(x) + c$$

$\cos \rightarrow \sin$

$$\int f'(x) \sec^2 f(x) dx = \tan f(x) + c$$

$$\int f'(x) e^{f(x)} dx = e^{f(x)} + c$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + c$$

$$\int f'(x) a^{f(x)} dx = \frac{a^{f(x)}}{\ln a} + c$$

$$\int \frac{f'(x)}{\sqrt{a^2 - [f(x)]^2}} dx = \sin^{-1} \frac{f(x)}{a} + c$$

$$\int \frac{f'(x)}{a^2 + [f(x)]^2} dx = \frac{1}{a} \tan^{-1} \frac{f(x)}{a} + c$$

$$\int u \frac{dv}{dx} dx = uv - \int v \frac{du}{dx} dx$$

$$\int_a^b f(x) dx$$

$$\approx \frac{b-a}{2n} \{f(a) + f(b) + 2[f(x_1) + \dots + f(x_{n-1})]\}$$

where $a = x_0$ and $b = x_n$

$y' = 0$ stationary point
 increase $y'(x) = +$
 decrease $y'(x) = -$
 concavity $y'' > 0 \rightarrow \cup$
 $y'' < 0 \rightarrow \cap$
 $m = y'(a)$ at point a